

ITB formation by toroidal momentum injection in flux-driven gyrokinetic turbulence

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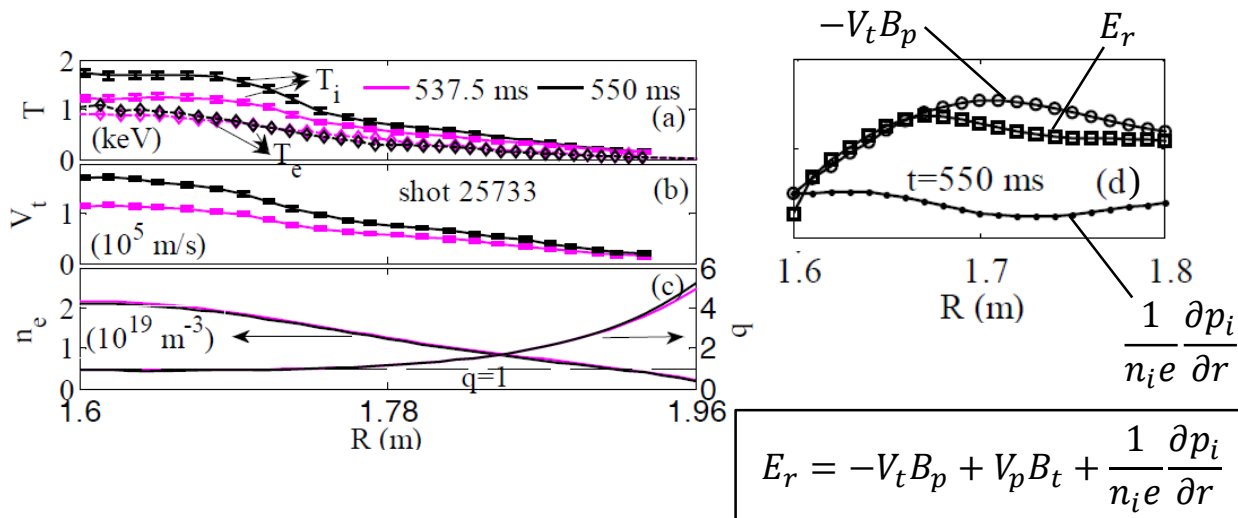
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2) *Southwestern Institute of Physics, China*

Background: ITB Formation in Weak/Reversed Magnetic Shear Plasma

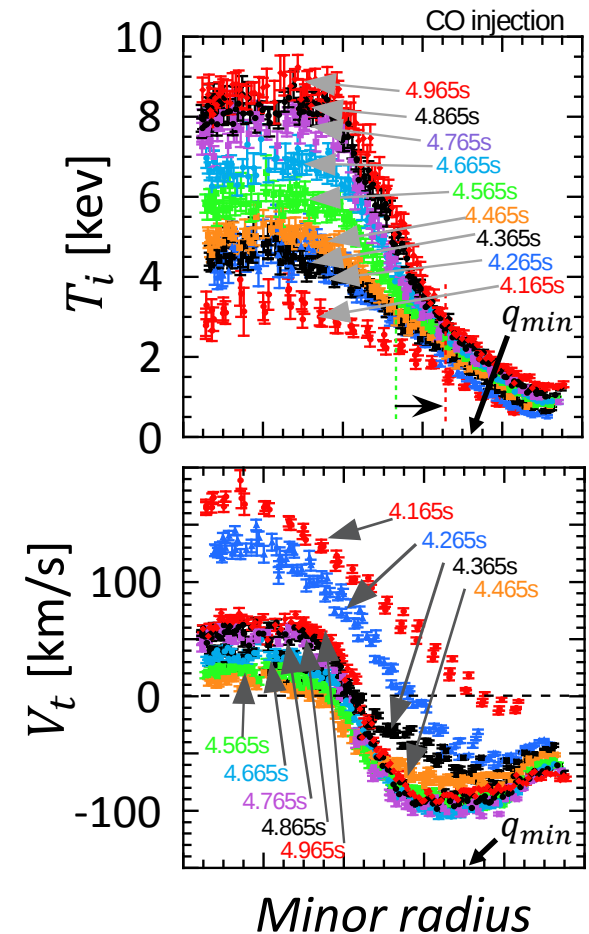
- ✓ ITB is formed in the recent **HL-2A weak magnetic shear discharges**. They found that **mean flow triggered by toroidal rotation plays a dominant role in sustaining ITB**.
- ✓ Clear box-type ITB is formed in the **JT-60U reversed shear discharges**, in which **co-input is more beneficial for ITB formation than counter-input**.

HL-2A (weak shear, Co)



[D. L. Yu, *et al.*, EX/8-2, 26th IAEA-FEC (2016).]

JT-60U (reversed shear, Co)



[Courtesy of Y. Sakamoto, QST]

Purpose of This Work

Purpose of this work

- ✓ Understanding the underlying mechanism of ITB formation in global gyrokinetic ITG turbulence

Radial force balance

$$E_r = -\frac{T_i}{e} \left(\frac{1}{L_{n_i}} + \frac{1-k}{L_{T_i}} \right) + \frac{rB}{qR} U_{\parallel}$$

Approaches

1. Non-local first-order ballooning theory

- ✓ Notation of θ_b , Δr and γ
- ✓ Impact of mean flow

2. Linear/Nonlinear global GK ITG simulation

- ✓ Impact of mean flow

3. Toroidal momentum injection

- ✓ Impact of toroidal momentum injection
- ✓ Hysteresis nature in the modulation test

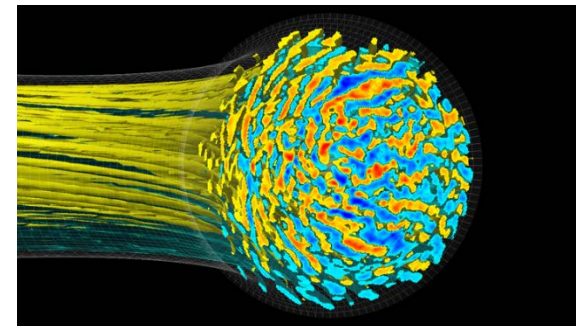
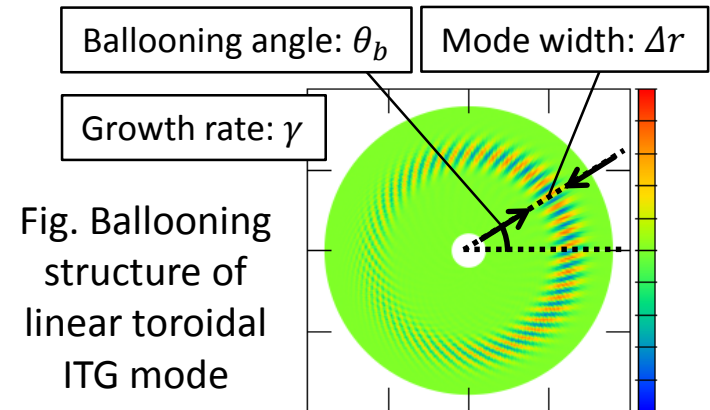


Fig. Typical structure of flux-driven toroidal ITG turbulence calculated by *GKNET*

Non-Local Ballooning Theory

[Y. Kishimoto, *et.al.*, Plasmas Phys. Controlled Fusion **40**, A663 (1998).]

$$\theta_b = \mp \left| \frac{\partial_r(\omega_r + \omega_f)}{2k_\theta \gamma_0 \hat{s}} \right|^{1/3}$$

$$\Delta r = \left| \frac{\sin \theta_b}{k_\theta^2 \hat{s}^2 \theta_b^3} \right|^{1/2}$$

$$\gamma = \gamma_0 \cos \theta_b$$

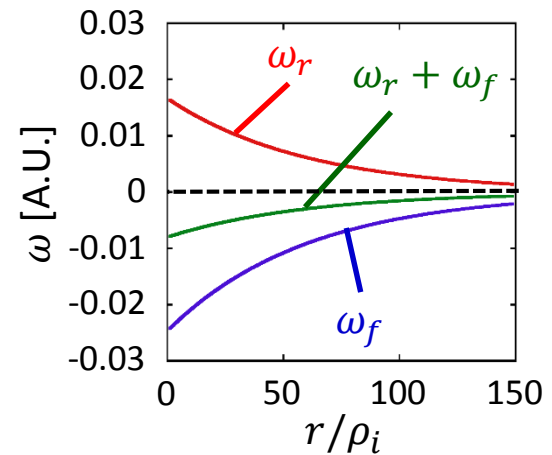
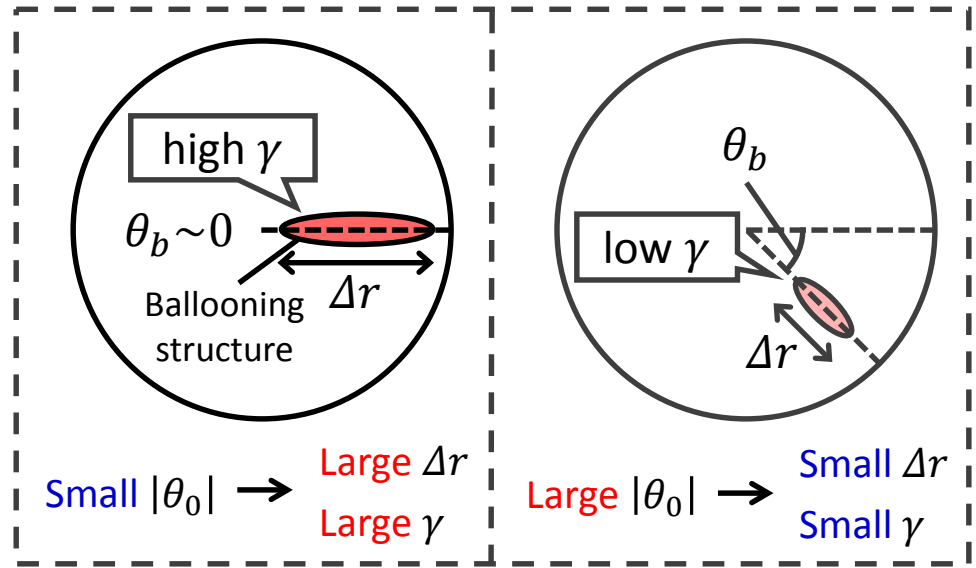
Radial force balance

$$E_r = \frac{rB}{qR} U_\parallel - \frac{T_i}{e} \left(\frac{1}{L_{n_i}} + \frac{1-k}{L_{T_i}} \right) \left(\begin{array}{l} n_i = n_{i0} \exp(-r/L_{n_i}) \\ T_i = T_{i0} \exp(-r/L_{T_i}) \end{array} \right)$$

Eigenfrequency + Doppler shift frequency

$$\omega_r + \omega_f \sim \frac{k_\theta}{eB} \left[\left(\frac{2}{R_0} - \frac{1}{L_{n_i}} - \frac{1-k}{L_{T_i}} \right) T_i - \frac{erB}{qR} U_\parallel \right]$$

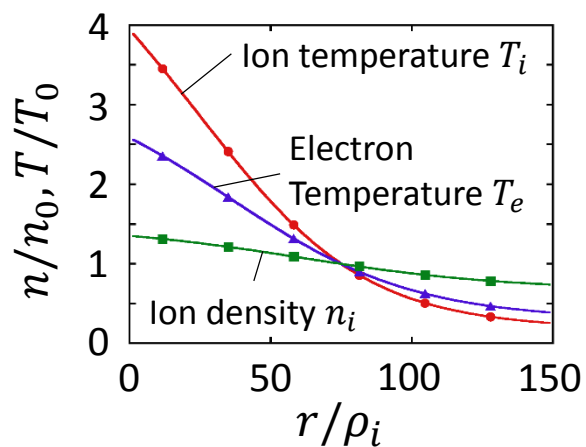
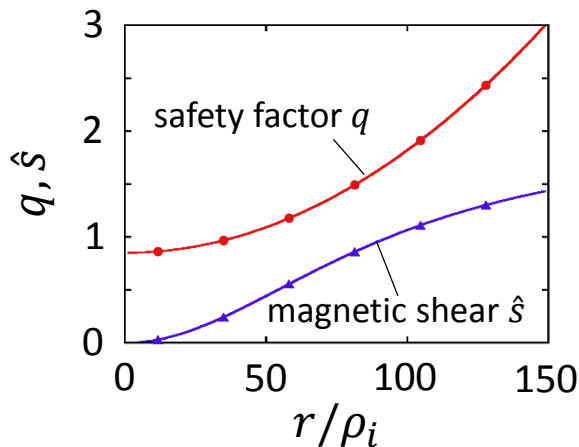
Diamagnetic drift *Mean flow* *Toroidal rotation*



- ✓ Cancellation by mean flow
- ✓ Impact of toroidal rotation

Nonlinear Flux-Driven GK ITG Simulation

Simulation condition



Parameter	Value
a_0/ρ_i	150
a_0/R_0	0.36
$(R_0/L_n)_{r=a_0/2}$	2.22
$(R_0/L_{T_i})_{r=a_0/2}$	10.0
$(R_0/L_{T_e})_{r=a_0/2}$	6.92
v_*	0.28
P_{in}	4, 8, 16, 24 [MW]

Source operator

$$S_{src} = A_{src}(r)\tau_{src}^{-1}[f_M(2\bar{T}) - f_M(\bar{T})]$$

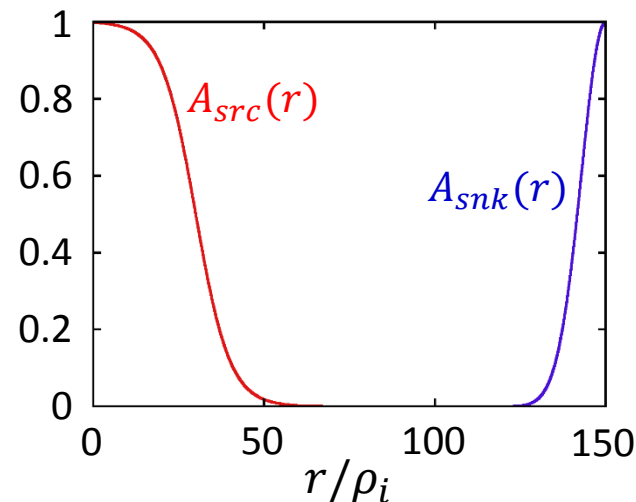
✓ Constant power input near magnetic axis

Sink operator

$$S_{snk} = A_{snk}(r)\tau_{snk}^{-1}[f(t) - f(t=0)]$$

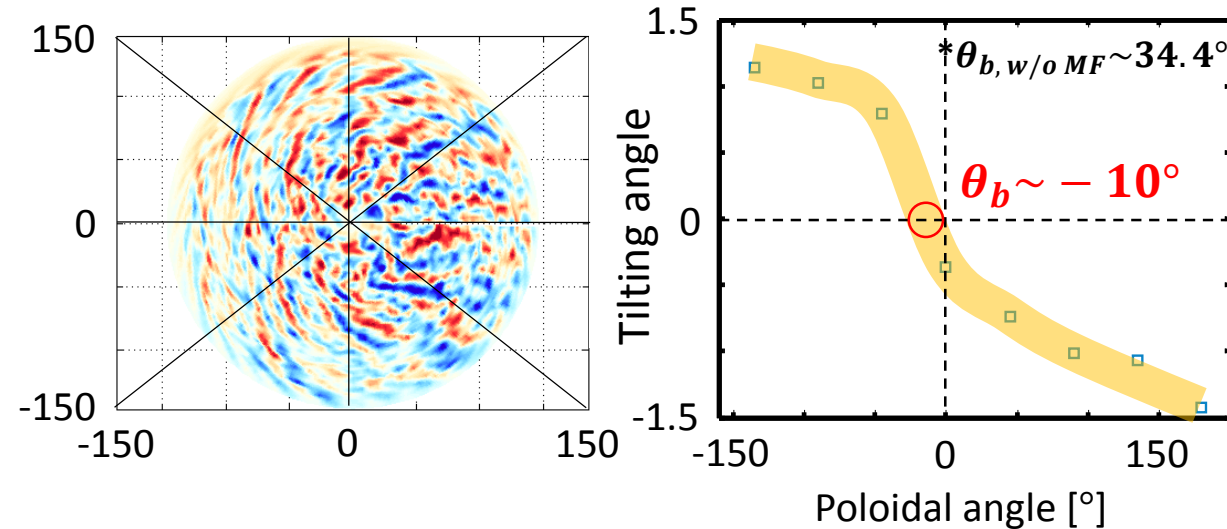
✓ Krook-type operator to f in boundary region

[Y. Idomura, *et. al.*, Nucl. Fusion, **49**, 065029 (2009).]

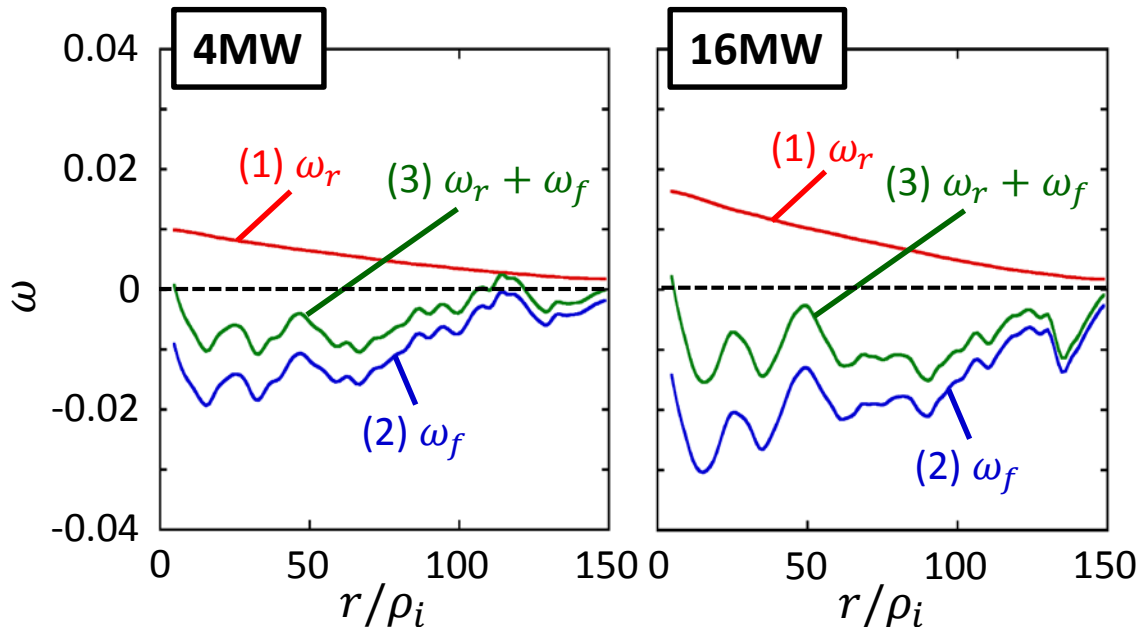


Poloidal Symmetry and Profile Stiffness

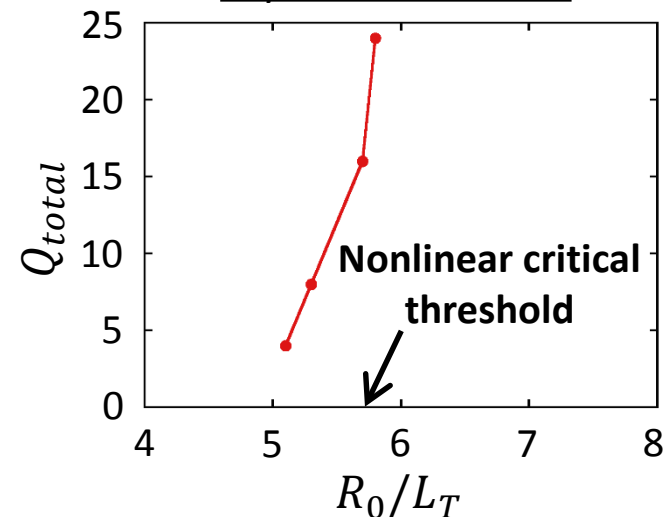
2D spatial correlation analysis for potential structure (16MW)



✓ **Ballooning angle is smaller** than that estimated from linear analysis without E_r .

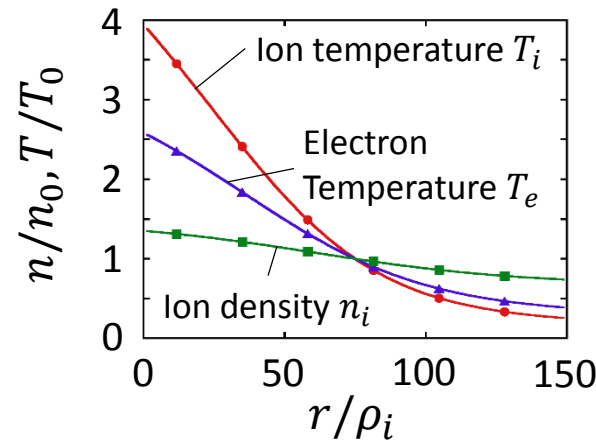
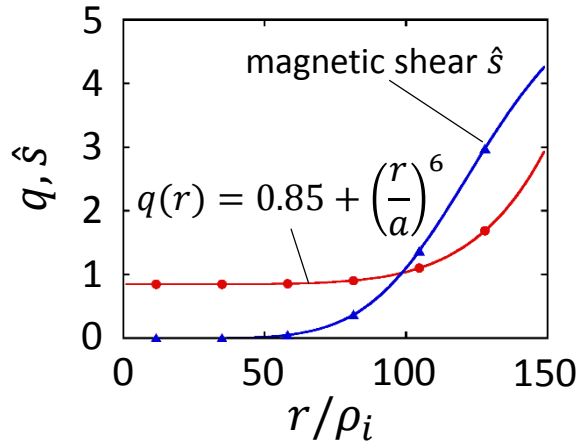


Gradient-Flux relation in power scan test



Flux-Driven ITG Simulation with Momentum Source by GKNET

Simulation condition



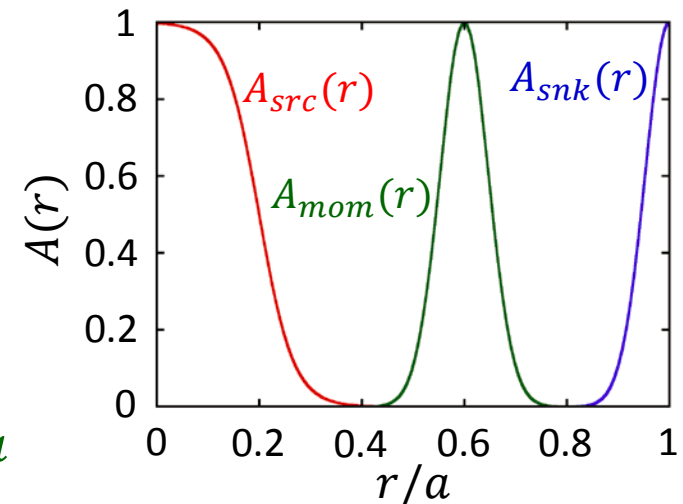
Parameter	Value
a_0/ρ_i	150
a_0/R_0	0.36
$(R_0/L_{n_i})_{r=a_0/2}$	2.22
$(R_0/L_{T_i})_{r=a_0/2}$	10.0
$(R_0/L_{T_e})_{r=a_0/2}$	6.92
v_*	0.28
P_{in}	4 [MW]
T_{in}	11.2 [N·m]

Momentum source operator

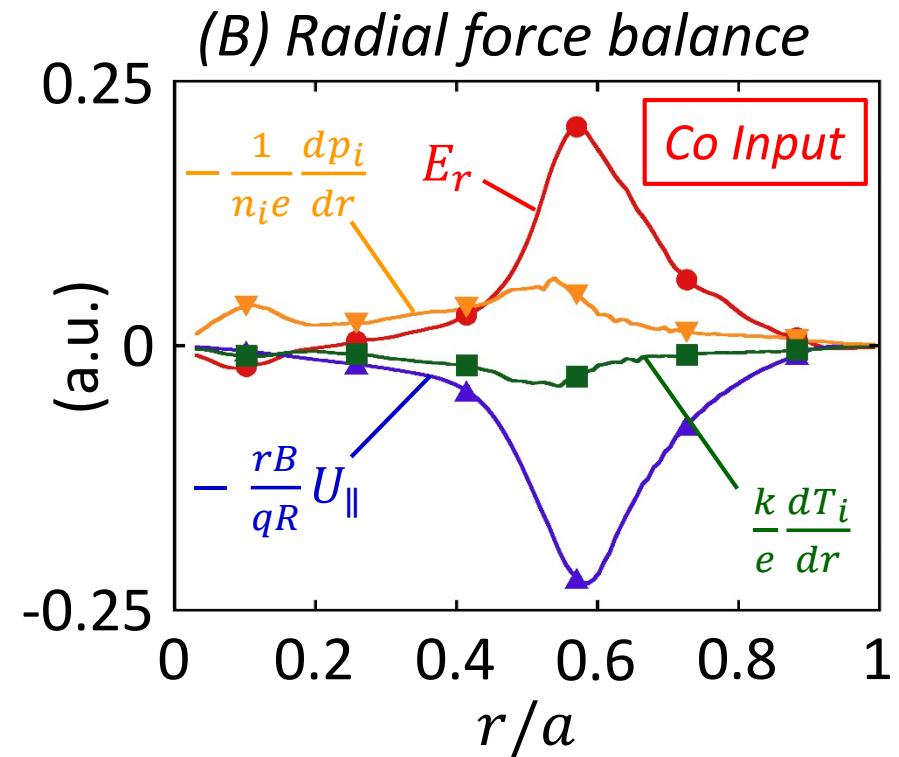
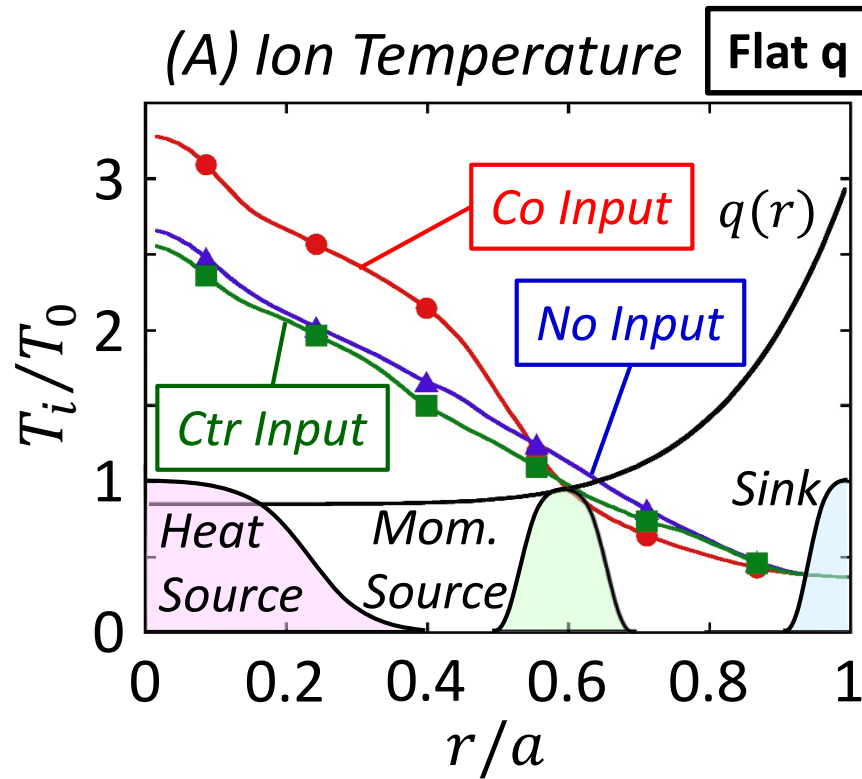
$$S_M = \tau_M^{-1} A(r) [f_{LM}(n_0, 0.5v_{ti}, T_0) - f_{LM}(n_0, 0, T_0)]$$

$$f_{LM}(n, U_{\parallel}, T) = \frac{n}{\sqrt{2\pi T^3/m_i^3}} \exp\left[-\frac{0.5(v_{\parallel} - U_{\parallel})^2 + \mu B}{T/m_i}\right]$$

- ✓ We compare three cases;
 - (A) without momentum source
 - (B) with co momentum source at $r = 0.6a$
 - (C) with counter momentum source at $r = 0.6a$



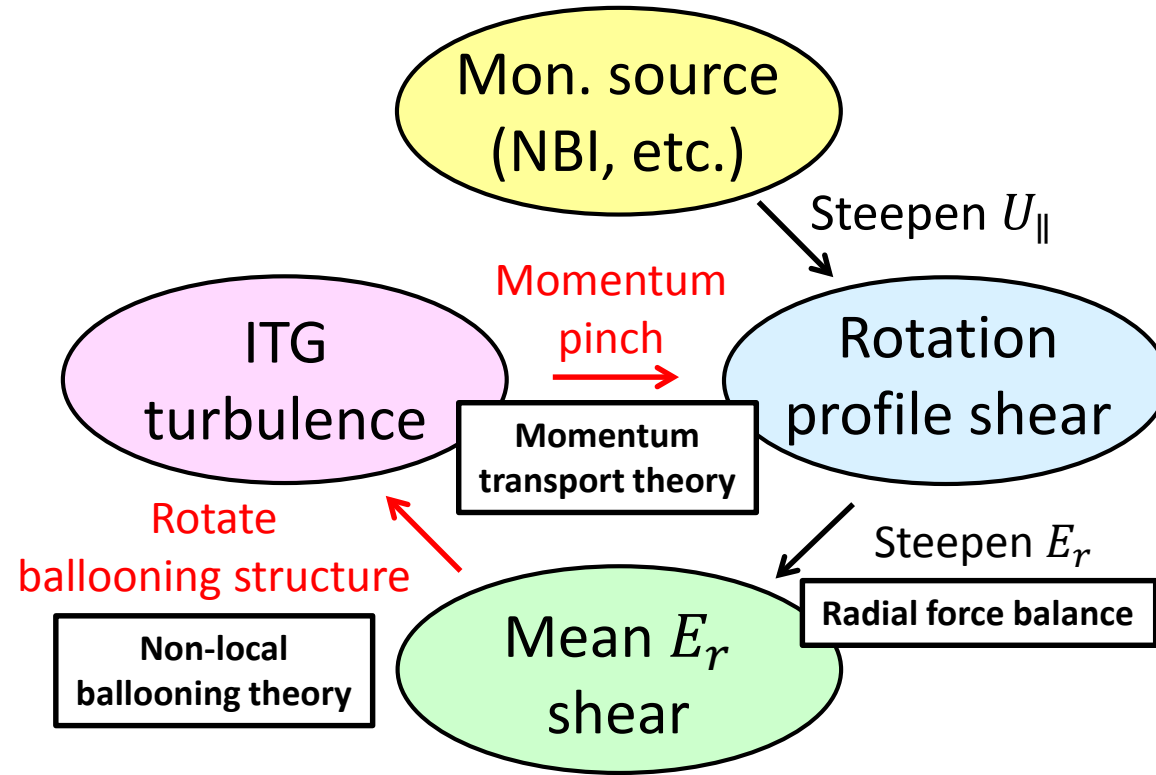
Effect of Rotation Direction



✓ Only co-current toroidal rotation can benefit the ITB formation in weak magnetic shear plasma.

→ qualitative agreement with the observations in the JET experiment

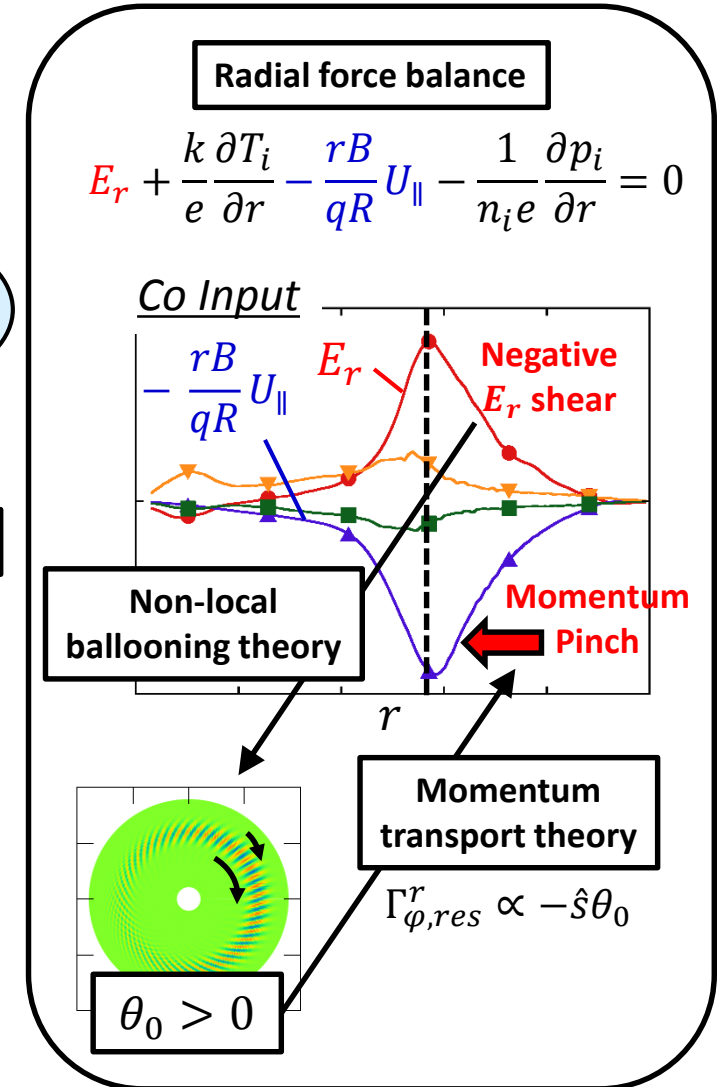
Feedback Loop between Mean E_r Shear and Momentum Pinch



Momentum transport theory

$$R_{\phi} \equiv \frac{\Gamma_{\phi}^r}{Q_i^r} \frac{v_{ti}}{R_0} = \frac{2}{R/L_T} \frac{\chi_{\phi}}{\chi_i} \left[u' + \frac{R_0 V_{co}}{\chi_{\phi}} u + \frac{C^*}{\chi_{\phi}} \right]$$

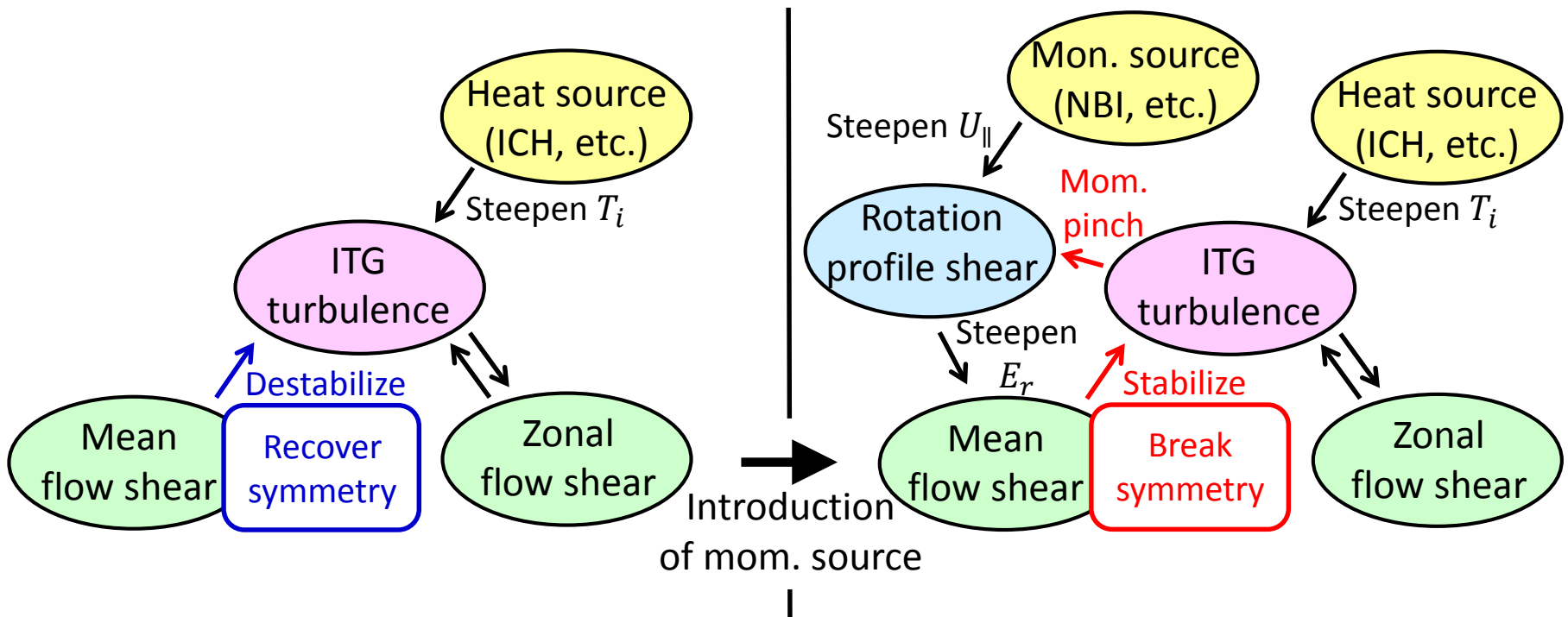
$$\frac{C^*}{\chi_{\phi}} \sim -\frac{\hat{s}}{2qk_{\theta}\rho_{ti}} \left[\frac{R_0}{L_n} + 4 \right] \theta_0$$



Summary & Future Plans - 1

Summary

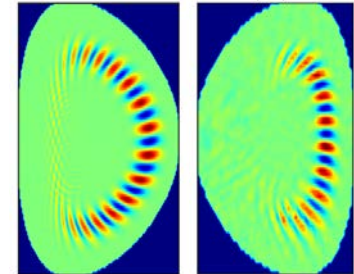
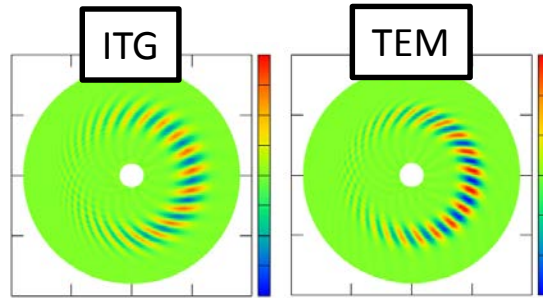
- ✓ We found that a momentum source can change the mean E_r through the radial force balance, **leading to ITB formation**.
- ✓ The underlying mechanism is identified to originate from **a positive feedback loop between the enhanced mean E_r shear and resultant momentum pinch**, which can be observed **only in co-input case**.



Summary & Future Plans - 2

Future plans

[K. Obrejan *et al*, Comput. Phys. Comm. **216**, 8 (2017).]



ITB formation in
flux-driven ITG turbulence

Introduction of
kinetic electron

Magnetic shaping effect
on ZF/GAM dynamics

ITB formation in
flux-driven ITG/TEM turbulence

- ✓ Opposite ballooning angle
- ✓ Density transport
- ✓ Momentum transport

Magnetic shaping effect
on ITG/TEM instability

- ✓ Impact of elongation and triangularity on ITG/TEM turbulence

Control of barrier formation by multi-sources and magnetic shape